

# Fast Collision Checking: From Single Robots to Multi-Robot Teams

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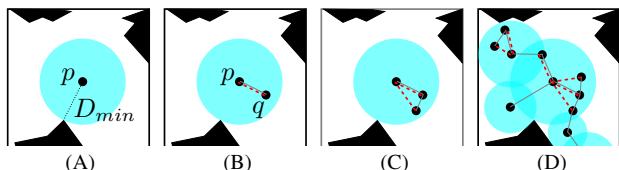
Collision checking is a critical bottle-neck in robotic motion planning and a key hurdle to enabling more sophisticated robotic systems [3]. Collision checking for a multi-robot team is even more difficult than for a single robot. In [1] we show that collision checking can be significantly reduced for a *single-robot* by using “safety certificates,” see Figure 1. We **now extend this result to centralized multi-robot teams**.

The configuration space of a multi-robot team is a Cartesian product of the space of each robot ( $R$  robots, each planning in  $D$ -dimensions, yields a  $RD$ -dimensional configuration space). Collision checking vs. the environment can be accomplished piecewise per robot. We evaluate three safety certificate methods for multi-robot teams: *Basic Certificate*, *Partial Certificate*, and *Shared Projection*—see Figure 2.

Figures 3 and 4 depict results from experiments using these methods with RRT [4] for teams of 1-5 robots. Note, RRT\* [2] gives similar results (these are omitted here due to space constraints). *Basic Certificate* suffers from a curse of dimensionality that limits its usefulness (Figure 3). Only *Shared Projection* provides significant runtime reductions for all team sizes (Figure 4). As in the single robot version of this work, there is eventually a graph size for which using certificates becomes more expensive than a tradition collision check. This appears to happen more quickly for *Shared Projection*, likely because *Shared Projection* adds  $R$  nodes to the secondary kd-tree per sample.

## REFERENCES

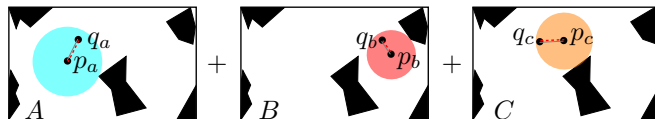
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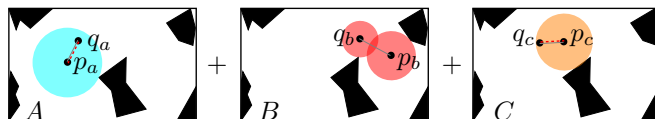
Collision checked nodes  $p$  store “safety certificates” (blue) defined by  $D_{min}$  the distance to the nearest obstacle (A). Future nodes  $q$  within a certificate can forgo collision checking (B). Pointer (red-dotted lines) are maintained to certifying nodes (C). The ratio of collision checks vs. all nodes approaches zero in the limit vs. graph size (D). See [1] for more details.

Fig. 1: Our Single-Robot Collision Certificate Method

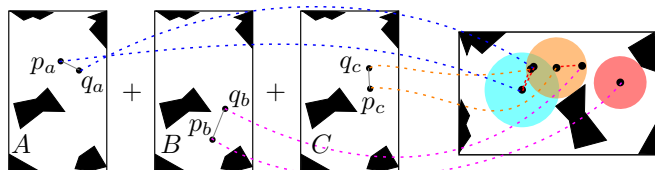
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**Basic Certificate:** Certificates are a Cartesian product of balls, one ball per robot. This is exactly [1] applied to a centralized multi-robot team. e.g.,  $q$  is certified safe by  $p$  if the projections  $q_a$ ,  $q_b$  and  $q_c$  are in the projected certificates of  $p_a$ ,  $p_b$  and  $p_c$  (blue, red, and orange balls), respectively.



**Partial Certificate:** If a point is *not* certified as safe with respect to a subspace projection, then only a partial collision check is required. e.g.,  $q_a$  and  $q_c$  are within the certificates of  $p_a$  and  $p_c$ , respectively, but  $q_b$  is not within the certificate of  $p_b$ . Thus, only 1/3 check is required (for  $q_b$ ).



**Shared Projection:** All robots collision check in the *same*  $D$ -dimensional projection (far right). This requires an *extra* kd-tree in the shared projected space, but time complexity only increases from  $\mathcal{O}(RD \log(N))$  to  $\mathcal{O}(RD \log(N) + D \log(R))$ , where  $D \log(R)$  is a constant. Pointers from configuration space node projections to their collision-checking projection counterparts are depicted with blue/magenta/orange dotted lines, respectively. Note that  $p_a$  certifies  $q_c$  and  $p_c$  certifies  $q_b$ .

Fig. 2: Our New Multi-Robot Collision Certificate Methods

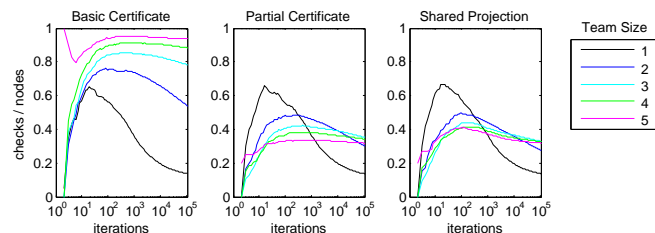


Fig. 3: Proportion of nodes requiring a collision check (mean value over 20 trials), lower values are better.

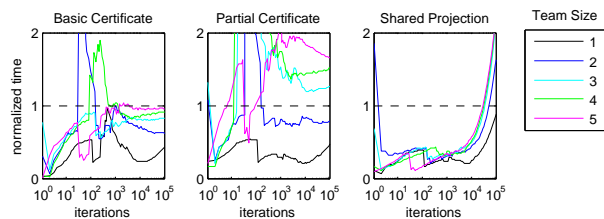


Fig. 4: Relative runtime of certificate methods vs. normal collision checking (mean over 20 trials), points below the dotted line are desired.